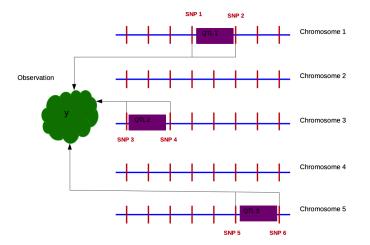
Genomic BLUP

Peter von Rohr

04.03.2019

- Estimate effect of few SNP loci linked to QTL
- Use parameter estimates to predict genomic breeding values
- New: Many SNP, find the important ones

Situation



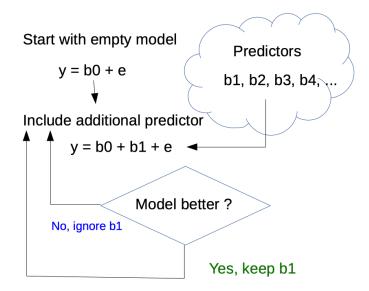
Goal: Find SNP 1 - SNP 6 out of the many SNPs

Approaches in Fixed Linear Model Framework

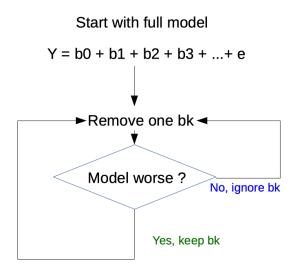
Two Approaches

- 1. Forward selection: Start with empty model, include predictors that improve model
- 2. Backward elimination: Start with full model, remove predictors as long as model does not get worse

Forward Selection



Backward Elimination



Model Selection With Genomic Data

- Only backward elimination really works in practical problems
- ► Large number of predictors (1.5 * 10⁵)
- How to determine sequence of predictors to eliminate
- Fitting the full model is problematic

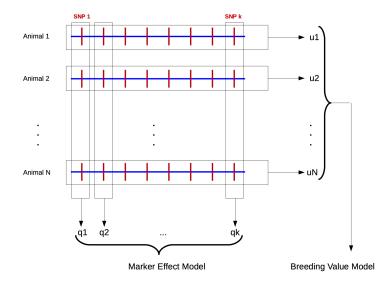
Mixed Linear Effect Model

- One solution: replace fixed linear effect model by mixed linear effect model (mle)
- MLE: additional random effect besides error term
- Random effects are specified by expected value and variance
- In livestock breeding MLE have a good reputation from BLUP animal model

MLE In Genomics

- Two different parametrizations
- 1. Marker Effect Model (MEM)
- 2. Breeding Value Model (BVM)

Overview



Marker Effect Model

In MEM random effects of markers are directly included in the model. For an idealized data set we can write

$$y = 1_n \mu + Wq + e$$

where

- y vector of length *n* with observations
- μ $\,$ general mean denoting fixed effects $\,$
- 1_n vector of length *n* of all ones
- q vector of length m of random SNP effects
- W design matrix relating SNP-genotypes to observations
- e vector of length *n* of random error terms

Breeding Value Model

$$y = Xb + Zg + e$$

where

- y vector of length *n* with observations
- b vector of length r with fixed effects
- X incidence matrix linking elements in b to observations
- g vector of length t with random genomic breeding values
- Z incidence matrix linking elements in g to observations
- *e* vector of length *n* of random error terms