

# Livestock Breeding and Genomics - Exercise 12

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## Problem 1 Marker Effect Model

We are given the dataset that is shown in the table below. This dataset contains genotyping results of 10 for 2 SNP loci.

| Animal | SNP A | SNP B | Observation |
|--------|-------|-------|-------------|
| 1      | 0     | 0     | 156         |
| 2      | 1     | 0     | 168         |
| 3      | 0     | 1     | 161         |
| 4      | 1     | 0     | 164         |
| 5      | -1    | 0     | 128         |
| 6      | -1    | 1     | 124         |
| 7      | 0     | -1    | 143         |
| 8      | 1     | 1     | 178         |
| 9      | 1     | 0     | 163         |
| 10     | 0     | 0     | 151         |

### Your Task

- The goal of this problem is to estimate SNP marker effects using a **marker effect model**. Because we have just 2 SNP loci, you can use a fixed effects linear model with the 2 loci as fixed effects. Furthermore you can also include a fixed intercept into the model.
- Specify all the model components including the vector of observations, the design matrix  $X$ , the vector of unknowns and the vector of residuals.
- You can use the R-function `lm()` to get the solutions for estimates of the unknown SNP effects.

### Your Solution

## Problem 2 Breeding Value Model

Use the same data as in Problem 1 to estimate genomic breeding values using a **breeding value model**.

### Hints

- The only fixed effect in this model is the mean  $\mu$  which is the same for all observations.
- You can use the following matrix as the genomic relationship matrix

$$G = \begin{bmatrix} 0.141 & -0.124 & -0.123 & -0.124 & 0.288 & 0.083 & 0.287 & -0.329 & -0.124 & 0.082 \\ -0.124 & 0.760 & -0.330 & 0.701 & -0.949 & -1.155 & 0.082 & 0.495 & 0.701 & -0.124 \\ -0.123 & -0.330 & 0.757 & -0.330 & 0.085 & 0.905 & -0.943 & 0.491 & -0.330 & -0.123 \\ -0.124 & 0.701 & -0.330 & 0.760 & -0.949 & -1.155 & 0.082 & 0.495 & 0.701 & -0.124 \\ 0.288 & -0.949 & 0.085 & -0.949 & 1.584 & 1.322 & 0.492 & -1.152 & -0.949 & 0.288 \\ 0.083 & -1.155 & 0.905 & -1.155 & 1.322 & 2.202 & -0.738 & -0.333 & -1.155 & 0.083 \\ 0.287 & 0.082 & -0.943 & 0.082 & 0.492 & -0.738 & 1.576 & -1.148 & 0.082 & 0.287 \\ -0.329 & 0.495 & 0.491 & 0.495 & -1.152 & -0.333 & -1.148 & 1.374 & 0.495 & -0.329 \\ -0.124 & 0.701 & -0.330 & 0.701 & -0.949 & -1.155 & 0.082 & 0.495 & 0.760 & -0.124 \\ 0.082 & -0.124 & -0.123 & -0.124 & 0.288 & 0.083 & 0.287 & -0.329 & -0.124 & 0.141 \end{bmatrix}$$

### Your Tasks

- Specify all model components of the linear mixed model, including the expected values and the variance-covariance matrix of the random effects.

### Your Solution