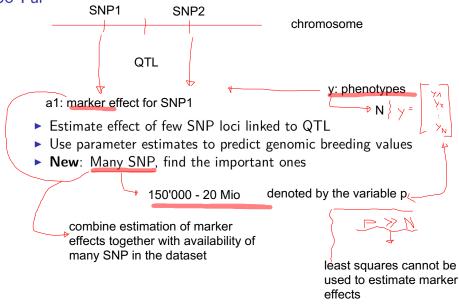
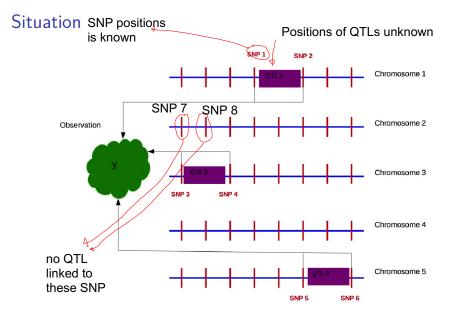


Peter von Rohr

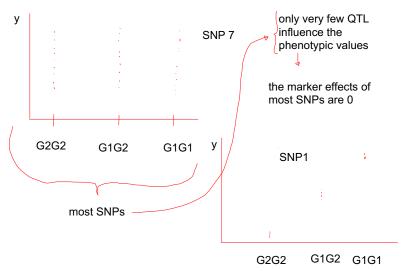
2021-03-08







Goal: Find SNP 1 - SNP 6 out of the many SNPs



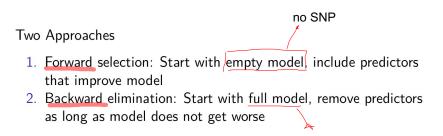
#### For the two SNPs 7 and 8 that are not linked to a QTL

Summary: 2 Problems 1. if we consider all SNP in our data set, then p>>N ==> least squares cannot be used 2. from genetic model: only few QTL for a given trait, ==> most SNP have marker effects (a) = 0

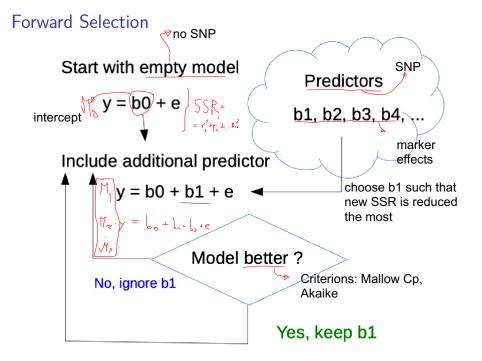
because the position of the QTL is unknown, we do not know which SNP have marker effects = 0

#### Approaches in Fixed Linear Model Framework

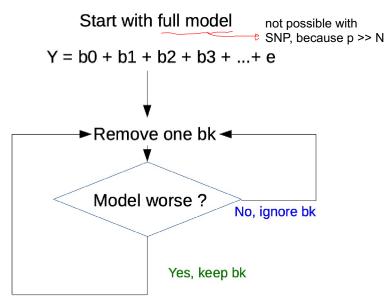
Possible solution for problem 2: Model selection to determine which SNP have marker effect that are not 0



all SNP, not possible due to p>>N



# Backward Elimination except for SNP data, this is the preferred way



## Model Selection With Genomic Data

cannot use backward elimination with genomic data, because parameter estimation in the full model cannot be

- Only backward elimination really works in practical problems
- Large number of predictors (1.5 \* 10<sup>5</sup>)
- How to determine sequence of predictors to eliminate
- Fitting the full model is problematic

## Mixed Linear Effect Model

2 Problems:

1. number of parameters p >> number of observations

2. only few SNP are important

- One solution: replace fixed linear effect model by mixed linear effect model (mle)
- ► MLE: additional random effect besides error term
- Random effects are specified by expected value and variance
- In livestock breeding MLE have a good reputation from BLUP animal model

# MLE In Genomics

two different types of model are different in their choice of random effects:

- 1. MEM: marker effects (a-values of the SNP) are taken to be random
- 2. BVM: genomic breeding value are taken as random

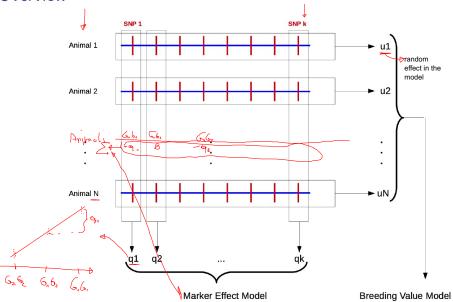
direct prediction of genomic breeding values without estimating marker effects

- Two different parametrizations
- 1. Marker Effect Model (MEM)
- 2. Breeding Value Model (BVM)

similar to the FLEM: 1. estimate marker effects 2. compute genomic breeding based on

the estimated marker effects

Overview



#### Marker Effect Model

In MEM random effects of markers are directly included in the model. For an idealized data set we can write

$$y = \underline{1_n \mu} + Wq + e$$

where

- y vector of length *n* with observations
- $\mu$  ~ general mean denoting fixed effects
- $1_n$  vector of length *n* of all ones
- q vector of length m of random SNP effects
- W design matrix relating SNP-genotypes to observations
- e vector of length n of random error terms

E(q) = (0); vor  $(q_{f}) = \int bq^{2}$ 

Breeding Value Model  $E(\underline{s}) = \emptyset$  $\sqrt{\alpha}(\underline{s}) = \underline{G} \cdot \overline{b},$ 

genomic relationship matrix

$$y = Xb + Zg + e$$

where

- y vector of length *n* with observations
- *b* vector of length *r* with fixed effects
- *X* incidence matrix linking elements in *b* to observations
- *g* vector of length *t* with random genomic breeding values
- Z incidence matrix linking elements in g to observations
- *e* vector of length *n* of random error terms