Selection Index

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So far ...

- Prediction of breeding values based on regression approach
- Usage of single class of information
 - own performance on the same trait
 - repeated measures
 - offspring records
- \rightarrow How to combine different sources of information

Desired Scenario



Two Approaches

- 1. Selection Index Theory and
- 2. Best Linear Unbiased Prediction (BLUP)
- Same genetic model
- Main difference in how identifiable environment is corrected for
- Start with 1. then move to 2.
- Nowadays 2. is most widely used method

Differentiate between

true breeding value: measures genetic potential, but cannot be observed

predicted breeding value: use information, such as phenotypic observations to predict true breeding value as accurate as possible

Three objectives of predicted breeding values

- 1. selection criterion for parents of next generation
- 2. prediction of true breeding value as early as possible
- 3. predicted breeding values affect price of semen and breeding animals

Selection Index Method



What is the Selection Index

- Combine all available information
- Assign single number I to each animal
- Rank animals according to I
- Use ranking as selection criterion
- Weights b_t for each information
- Determine weights b How To? Follows

Aggregate Genotype

- Want to improve more than just one trait
- How to select animals?



Selection Methods

- Tandem selection: First improve only trait 1, then improve only trait 2
- Independent selection boundaries: select for trait 1, among selected look at trait 2
- Combine traits into aggregate genotype H

$$H = w_1 a_1 + w_2 a_2 + \cdots + w_m a_m = w^T a$$

where *a* vector of true breeding values *w* vector of economic values

Economic Values

- Change in profit when trait changes
- How does the profit change when animals
 - are healthier or
 - produce more or
 - reduce environmental impact

Change in Profit



K1: costs for producing a product that is in this first category E1: revenue obtained by selling products of the first category G1: profit

Selection Index Construction

- Index Construction means: finding unknown vector of weights b in I
- Objective: I has to approximate H as good as possible
- Criterion:

$$E(H-I)^2 \rightarrow \min$$

Result: Index normal equations

$$Pb = Gw$$

Solution

Compute b from index normal equation

$$Pb = Gw$$

 $P^{-1}Pb = P^{-1}Gw$
 $b = P^{-1}Gw$

Accuracy of index I

$$r_{HI} = \frac{cov(H, I)}{\sigma_H \sigma_I} = \frac{\sigma_I}{\sigma_H}$$