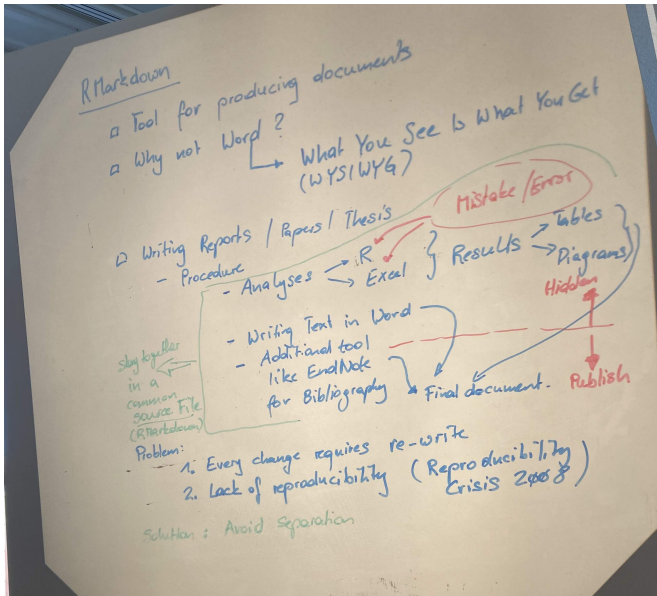


# OHP Page 1

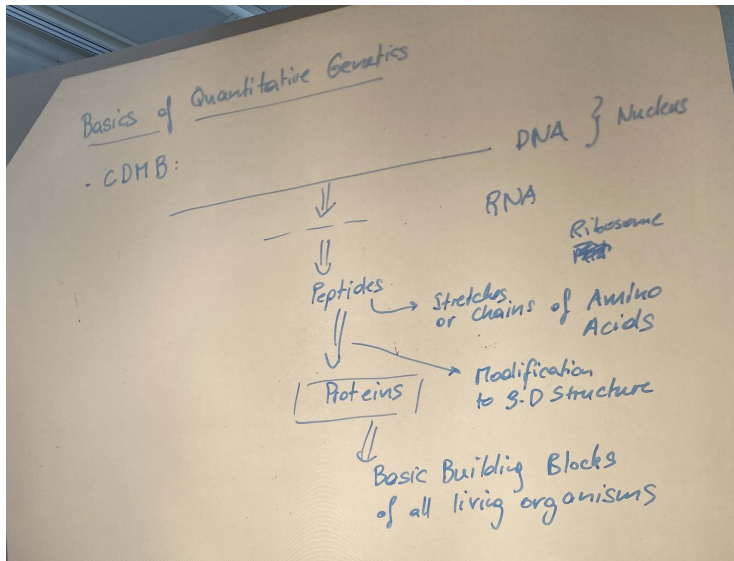


R Markdown as an example of a unified source file

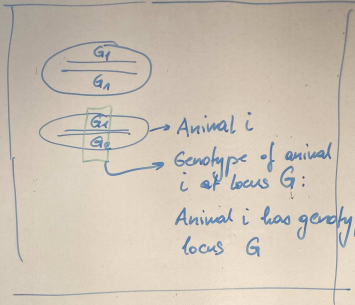
- Not WYSIWYG (other examples: HTML websites)
- Source file with special characters that are defining the structure of the document
- Information of the document is separated from its appearance.

Rmd Format:

- URLs
- `**text**` → bold
- `*text*` ⇒ italics
- `"{ r name }` ⇒ R-code chunk start
- `"` ⇒ R-code chunk end



Population : Given locus  $G$  with two alleles  $G_1$  and  $G_2$



Two different alleles  $G_1$  and  $G_2$  might come from ~~the~~ a difference in the sequence of DNA bases.

- At level of genotypes the order is not important.  
Genotypes  $G_1G_2 \equiv G_2G_1$
- Based on genotype, parental origin of the alleles is unknown.
- Only based on haplotype information, parental origin can be determined

## Frequencies of Genotypes

$$\begin{aligned}
 f(G_1G_1) &= \frac{\# G_1G_1}{N} = \frac{4}{10} = 0.4 \\
 f(G_1G_2) &= \frac{\# G_1G_2}{N} = \frac{3}{10} = 0.3 \\
 f(G_2G_1) &= \frac{\# G_2G_1}{N} = \frac{3}{10} = 0.3
 \end{aligned}
 \left. \begin{array}{l} \\ \\ \end{array} \right\} \begin{array}{l} \text{Sum:} \\ f(G_1G_1) + f(G_2G_1) \\ + f(G_2G_2) = 1 \end{array}$$

$\swarrow$  Number of  $\searrow$  total number of animals  
in the population

• Alleles:

$$\begin{aligned}
 f(G_1) &= \frac{\# G_1}{2N} = \frac{11}{20} = 0.55 \\
 f(G_2) &= \frac{\# G_2}{2N} = \frac{9}{20} = 0.45
 \end{aligned}
 \left. \begin{array}{l} \\ \end{array} \right\} f(G_1) + f(G_2) = 1$$

• Allele frequencies from Genotype frequencies  $f(G_1G_1)$

$$f(G_1) = \frac{\# G_1}{2N} = \frac{2N \cdot f(G_1G_1) + f(G_1G_2) \cdot N}{2N} = \frac{f(G_1G_1) + \frac{1}{2} f(G_1G_2)}{1}$$

$$\# G_1 = \underbrace{2 \cdot \# G_1G_1}_{\rightarrow N \cdot f(G_1G_1)} + 1 \cdot \# G_1G_2 \cdot f(G_1G_2) \cdot N$$

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## Hardy-Weinberg Equilibrium

- Given allele frequencies  $f(G_1) = p$   
 $f(G_2) = q$  }  $p+q=1$

- Resulting genotype frequencies under random mating and no selection (idealized population). Genotypes are the result of randomly combining gametes (eggs and sperm)

		egg	
		$G_1$	$G_2$
Sperm	$G_1$	$f(G_1G_1) = p \cdot p = p^2$	$f(G_1G_2) = p \cdot q$
	$G_2$	$f(G_2G_1) = q \cdot p = pq$	$f(G_2G_2) = q \cdot q = q^2$

Genotype frequencies:

$$f(G_1G_1) = p^2$$
$$f(G_1G_2) = 2p \cdot q$$
$$f(G_2G_2) = q^2$$

$$f(G_1G_1) + f(G_1G_2) + f(G_2G_1) + f(G_2G_2) = 1$$
$$p^2 + 2pq + q^2 = (p+q)^2 = 1$$

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- Genotype frequencies and allele frequencies remain constant over time

Population:  $f(G_1G_1) = p^2, f(G_1G_2) = 2pq, f(G_2G_2) = q^2$

Parents  
↓  
2nd generation

	$G_1$ $f(G_1) = p$	$G_2$ $f(G_2) = q$
$G_1$ $f(G_1G_1) = p^2$	$f(G_1G_1) = p^2$	$f(G_1G_2) = pq$
$G_2$ $f(G_2G_2) = q^2$	$f(G_2G_1) = pq$	$f(G_2G_2) = q^2$

$$f(G_1) = f(G_1G_1) + \frac{1}{2} f(G_1G_2)$$

$$= p^2 + \frac{1}{2} \cdot 2 \cdot p \cdot q = p^2 + p \cdot q$$

$$= p(p+q) = p$$

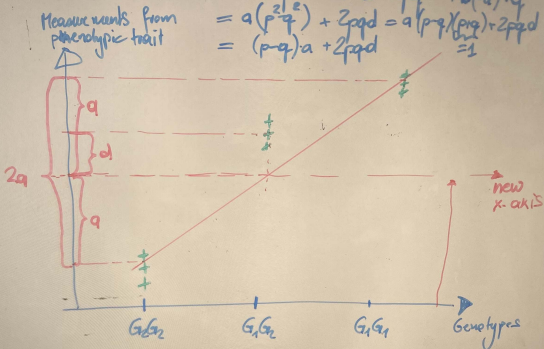
$$f(G_2) = f(G_2G_2) + \frac{1}{2} f(G_1G_2)$$

$$= q^2 + p \cdot q = q(q+p) = q$$

## Genotypic Values

- Expected value for the random variable  $V$  is the population mean:

$$\begin{aligned} \mu &= V_{11} \cdot f(G_1G_1) + V_{12} \cdot f(G_1G_2) + V_{22} \cdot f(G_2G_2) \\ &= a \cdot p^2 + d \cdot 2pq + (-a) \cdot q^2 \\ &= a(p^2 - q^2) + 2pqd = a(p-q)(p+q) + 2pqd \\ &= (p-q)a + 2pqd \end{aligned}$$



Genotypic value for  $G_1G_1$  is called  $V_{11} = a$   
 $G_1G_2$  is called  $V_{12} = d$   
 $G_2G_2$  is called  $V_{22} = -a$