# Livestock Breeding and Genomics - Exercise 2

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## Problem 1: Vectors in R

#### **Vector Definition**

Although there exists a function called vector() in R, vectors are always defined in R using the function c() which stands for "concatenation".

#### Vector Assignment

Let us assume we want to assign the following vector a

$$a = \left[ \begin{array}{c} 10\\7\\43 \end{array} \right]$$

to the variable named a in R, then this can be done with the following statement

a <- c(10,7,43)

#### Access of single Vector Element

A single vector element can be accessed using the variable name followed by the element index in brackets. Hence, if we want to know the first element of vector **a**, we have to write

a[1]

## [1] 10

#### **Computations with Vector Elements**

Vector elements can be used in arithmetic operations such as summation, subtraction and multiplication as shown below

a[1] + a[3]

## [1] 53

a[2] \* a[3] ## [1] 301 a[3] - a[1]

## [1] 33

The function **sum()** can be used to compute the sum of all vector elements. The function **mean()** computes the mean of all vector elements.

sum(a)			
## [1] 60			
mean(a)			
## [1] 20			

### Vector Computations

Arithmetic operations can also be performed not only on elements of vectors but also on complete vectors. Hence, we can add the vector **a** to itself or we can multiply it by a factor of 3.5 which is shown in the following code-chunk

a + a

## [1] 20 14 86

## **3.5** \* a

## [1] 35.0 24.5 150.5

#### More Computations on Vectors

Given are the following two vectors v and w.

$$v = \begin{bmatrix} 3\\ -5\\ 1\\ 9 \end{bmatrix}$$
$$w = \begin{bmatrix} 1\\ 9\\ -12\\ 27 \end{bmatrix}$$

Compute

- the sum v + w,
- the difference v w and
- the dot product  $v \cdot w$ .

## Problem 2: Matrices in R

Matrices in R are defined using the function matrix(). The function matrix() takes as first arguments all the elements of the matrix as a vector and as further arguments the number of rows and the number of columns. The following statement generates a matrix with 4 rows and 3 columns containing all integer numbers from 1 to 12.

```
mat_by_col <- matrix(1:12, nrow = 4, ncol = 3)
mat_by_col</pre>
```

```
[,1] [,2] [,3]
##
## [1,]
             1
                   5
                         9
## [2,]
             2
                   6
                       10
## [3,]
             3
                   7
                       11
## [4,]
             4
                   8
                       12
```

As can be seen, the matrix elements are ordered by columns. Often, we want to define a matrix where elements are filled by rows. This can by done using the option byrow=TRUE

```
mat_by_row <- matrix(1:12, nrow = 4, ncol = 3, byrow = TRUE)
mat_by_row</pre>
```

```
[,1] [,2] [,3]
##
## [1,]
             1
                   2
                         3
## [2,]
             4
                   5
                         6
## [3,]
             7
                   8
                         9
## [4,]
            10
                  11
                       12
```

#### Access of Matrix Elements

Matrix elements can be accessed similarly to what was shown for vectors. But to access a single element, we need two indices, one for rows and one for columns. Hence the matrix element in the second row and third column can be accessed by

mat\_by\_row[2,3]

## [1] 6

#### Arithmetic Computations with Matrices

Arithmetic computations with matrices can be done with the well-known operators as long as the matrices are compatible. For summation and subtraction matrices must have the same number of rows and columns. For matrix-multiplication, the number of columns of the first matrix must be equal to the number of rows of the second matrix.

In R the arithmetic operators +, - and \* all perform element-wise operations. The matrix multiplication can either be done using the operator %\*% or the function crossprod(). It has to be noted that the statement

crossprod(A, B)

computes the matrix-product  $A^T \cdot B$  where  $A^T$  stands for the transpose of matrix A. Hence the matrix product  $A \cdot B$  would have to be computed as

crossprod(t(A), B)

# More Examples

Given the matrices X and Y

X <- matrix(1:15, nrow = 5, ncol = 3) Y <- matrix(16:30, nrow = 5, ncol = 3)

Compute

- X + Y
- Y X
- multiplication of elements between X and Y matrix-product  $X^T \cdot Y$  matrix-product  $X^T \cdot X$  matrix-product  $Y^T \cdot Y$